

Computer Assignment 1

Chapter 1, section 1, problem 1a program file Ch1s1pb01a.m

```
A = [-1 2 1 0; 0 -2 -1 2; -1 1 0 3]

B=rowcomb(A,3,1,-2)
% The command rowcomb(A,i,j,c) forms a matrix
% from A by adding c times the ith row of A
% to the jth row.

C=rowscale(B,2,-1/2)
% The command rowscale(A,i,c) multiplies
% row i of the matrix A by the scalar c
% and outputs the resulting matrix.

D=rowcomb(C,1,3,1); D=rowcomb(D,2,3,-1)
E=rowscale(D,3,2)
F=rowcomb(E,3,2,-1/2); F=rowcomb(F,3,1,-1)
```

Result in Matlab

```
>> Ch1s1pb01a

A =
   -1     2     1     0
    0    -2    -1     2
   -1     1     0     3

B =
     1     0     1    -6
     0    -2    -1     2
    -1     1     0     3

C =
   1.0000         0   1.0000   -6.0000
         0   1.0000   0.5000   -1.0000
  -1.0000   1.0000         0    3.0000

D =
   1.0000         0   1.0000   -6.0000
         0   1.0000   0.5000   -1.0000
         0         0   0.5000   -2.0000

E =
   1.0000         0   1.0000   -6.0000
         0   1.0000   0.5000   -1.0000
         0         0   1.0000   -4.0000

F =
     1     0     0    -2
     0     1     0     1
     0     0     1    -4

>>
```

Reduced Row Echelon Form

One solution:

$$x_1 = -2$$

$$x_2 = 1$$

$$x_3 = -4$$

Chapter 1, section 1, problem 1b program file Ch1s1pb01b.m

```
A = [0 -1 -1 1;-1 0 1 0;1 -2 1 -1;1 -1 1 3]

B=rowswap(A,1,2)
% The command rowswap(A,i,j) interchanges
% rows i and j of the matrix A and outputs
% the resulting matrix.

C=rowscale(B,1,-1); C=rowscale(C,2,-1)
% The command rowscale(A,i,c) multiplies
% row i of the matrix A by the scalar c
% and outputs the resulting matrix.

D=rowcomb(C,1,3,-1); D=rowcomb(D,2,3,2)
% The command rowcomb(A,i,j,c) forms a matrix
% from A by adding c times the ith row of A
% to the jth row.

E=rowscale(D,3,1/4)
F=rowcomb(E,1,4,-1); F=rowcomb(F,2,4,1)
G=rowscale(F,4,1/3)
```

Result in Matlab

```
> Ch1s1pb01b

A =
     0     -1     -1     1
    -1     0     1     0
     1     -2     1    -1
     1     -1     1     3

B =
    -1     0     1     0
     0     -1    -1     1
     1     -2     1    -1
     1     -1     1     3

C =
     1     0    -1     0
     0     1     1    -1
     1     -2     1    -1
     1     -1     1     3

D =
     1     0    -1     0
     0     1     1    -1
     0     0     4    -3
     1     -1     1     3

E =
     1.00     0    -1.00     0
         0     1.00     1.00    -1.00
         0         0     1.00    -0.75
     1.00    -1.00     1.00     3.00

F =
     1.00     0    -1.00     0
         0     1.00     1.00    -1.00
         0         0     1.00    -0.75
         0         0     3.00     2.00

G =
     1.00     0    -1.00     0
         0     1.00     1.00    -1.00
         0         0     1.00    -0.75
         0         0     1.00     0.67

>
```

Row Echelon Form
It is not possible for
 $x_3 = -0.75$ and $x_3 = 0.67$
therefore the system is
inconsistent and there are
no solutions.

Chapter 1, section 1, problem 1c program file Ch1s1pb01c.m

```
A = [-1 3 2 -3;-2 6 3 -1]

B=rowscale(A,1,-1)
% The command rowscale(A,i,c) multiplies
% row i of the matrix A by the scalar c
% and outputs the resulting matrix.

C=rowcomb(B,1,2,2)
% The command rowcomb(A,i,j,c) forms a matrix
% from A by adding c times the ith row of A
% to the jth row.

D=rowscale(C,2,-1)
E=rowcomb(D,2,1,2)
```

Result in Matlab

» Ch1s1pb01c

```
A =
   -1     3     2    -3
   -2     6     3    -1
```

```
B =
     1    -3    -2     3
    -2     6     3    -1
```

```
C =
     1    -3    -2     3
     0     0    -1     5
```

```
D =
     1    -3    -2     3
     0     0     1    -5
```

```
E =
     1    -3     0    -7
     0     0     1    -5
```

»

Reduced Row Echelon Form

Infinite solutions:

$$x_1 = -7 + 3t_2$$

$$x_2 = t$$

$$x_3 = -5$$

Chapter 1, section 1, problem 1d program file Ch1s1pb01d.m

```
A = [3 2 1 8;0 -2 2 -2;-3 -1 -2 -7;3 1 2 7]

B=rowscale(A,1,1/3); B=rowscale(B,2,-1/2)
% The command rowscale(A,i,c) multiplies
% row i of the matrix A by the scalar c
% and outputs the resulting matrix.

C=rowcomb(B,4,3,1)
D=rowcomb(C,1,4,-3)
E=rowcomb(D,2,4,1)
F=rowcomb(E,2,1,-2/3)
% The command rowcomb(A,i,j,c) forms a matrix
% from A by adding c times the ith row of A
% to the jth row.
```

Result in Matlab

» Ch1s1pb01d

```
A =
    3     2     1     8
    0    -2     2    -2
   -3    -1    -2    -7
    3     1     2     7

B =
    1.0000    0.6667    0.3333    2.6667
         0    1.0000   -1.0000    1.0000
   -3.0000   -1.0000   -2.0000   -7.0000
    3.0000    1.0000    2.0000    7.0000

C =
    1.0000    0.6667    0.3333    2.6667
         0    1.0000   -1.0000    1.0000
         0         0         0         0
    3.0000    1.0000    2.0000    7.0000

D =
    1.0000    0.6667    0.3333    2.6667
         0    1.0000   -1.0000    1.0000
         0         0         0         0
         0   -1.0000    1.0000   -1.0000

E =
    1.0000    0.6667    0.3333    2.6667
         0    1.0000   -1.0000    1.0000
         0         0         0         0
         0         0         0         0

F =
    1     0     1     2
    0     1    -1     1
    0     0     0     0
    0     0     0     0

»
```

Reduced Row Echelon Form
Infinite solutions:
 $x_1 = 2 - t$
 $x_2 = 1 + t$
 $x_3 = t$

Chapter 1, section 1, problem 2 program file Ch1s1pb02.m

```
A = randint(3,4,5)
b = randint(3,1,5)
% RANDINT(m,n,k,r) is an m by n matrix of rank r
% with integer entries in the interval [-k:k].
% If less than three arguments are used the default
% value of k is taken to be 9.
% If only one input argument is used then it is assumed
% that the matrix is square.
% If the last argument is left off, no attempt is made
% to determine the rank.

C = rref(A)
% rref is Reduced Row Echelon Form
D = [A,b]
% I just want to see what [A,b] means
E = rref([A,b])
```

Result in Matlab

» Ch1s1pb02

```
A =
    0    -2     2    -4
    2    -3    -2     2
   -1    -3     0    -1

b =
    4
    4
    1

C =
    1.0000         0         0   -0.0909
         0    1.0000         0    0.3636
         0         0    1.0000  -1.6364

D =
    0    -2     2    -4     4
    2    -3    -2     2     4
   -1    -3     0    -1     1

E =
    1.0000         0         0   -0.0909    1.7273
         0    1.0000         0    0.3636   -0.9091
         0         0    1.0000  -1.6364    1.0909

»
```

Reduced Row Echelon Form

For $Ax = b$:

Infinite solutions:

$$x_1 = 1.7273 + 0.0909t$$

$$x_2 = -0.0901 - 0.3636t$$

$$x_3 = 1.0909 + 1.6364t$$

$$x_4 = t$$

For $Ax = 0$:

Infinite solutions:

$$x_1 = 0.0909t$$

$$x_2 = -0.3636t$$

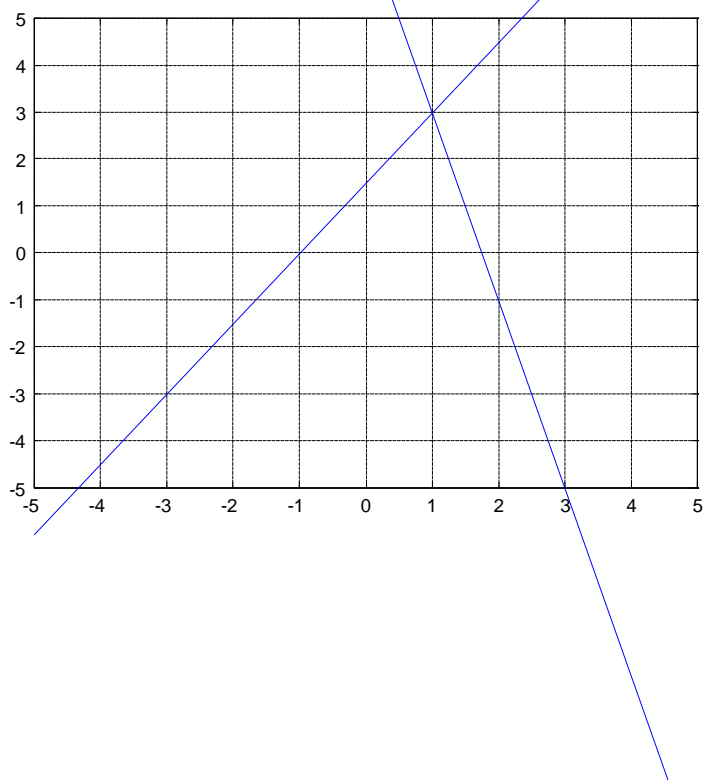
$$x_3 = 1.6364t$$

$$x_4 = t$$

Chapter 1, section 2, problem 1a program file Ch1s2pb01a.m

```
plotline(4,1,7)
% plotline(a,b,c,s)
% plots the line ax + by = c with axis
% set to [-s,s,-s,s]. If the last input
% arguments is omitted, its default value
% is taken to be 5.
hold on
% "hold on" permits an additional plot to be
% added to the current plot
plotline(3,-2,-3)
grid
% "grid" toggles whether grid lines are on or off
hold off
```

Result in Matlab



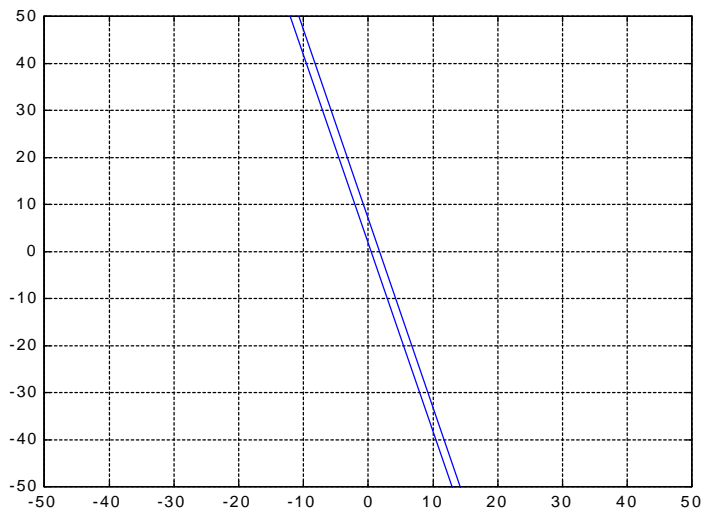
One solution:

$$x = 1$$
$$y = 3$$

Chapter 1, section 2, problem 1b program file Ch1s2pb01b.m

```
plotline(4,1,7,50)  
hold on  
plotline(-8,-2,-4,50)  
grid  
hold off
```

Result in Matlab

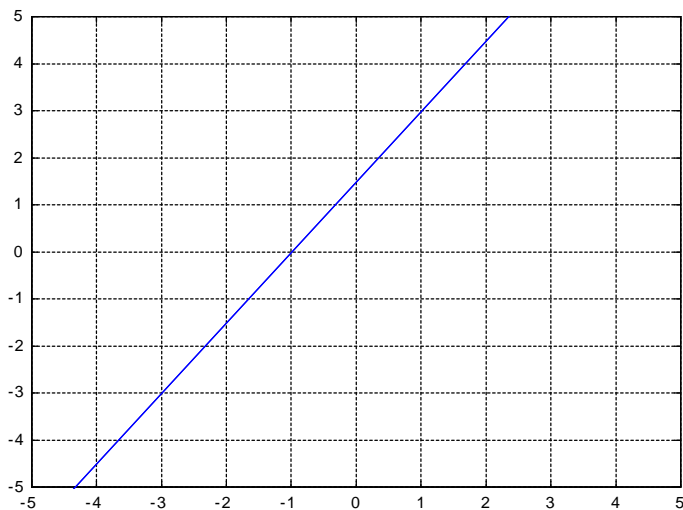


No solutions:
(parallel lines)

Chapter 1, section 2, problem 1c program file Ch1s2pb01c.m

```
plotline(3,-2,-3)  
hold on  
plotline(-6,4,6)  
grid  
hold off
```

Result in Matlab

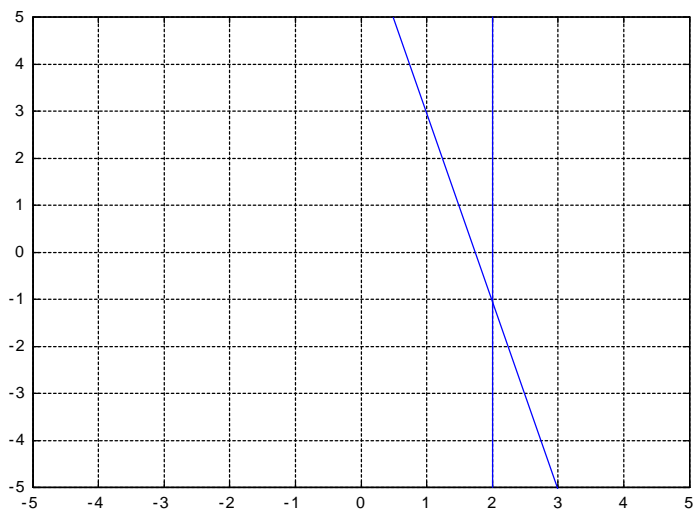


Infinite solutions:
2 overlying lines

Chapter 1, section 2, problem 1d program file Ch1s2pb01d.m

```
plotline(4,1,7)  
hold on  
plotline(1,0,2)  
grid  
hold off
```

Result in Matlab

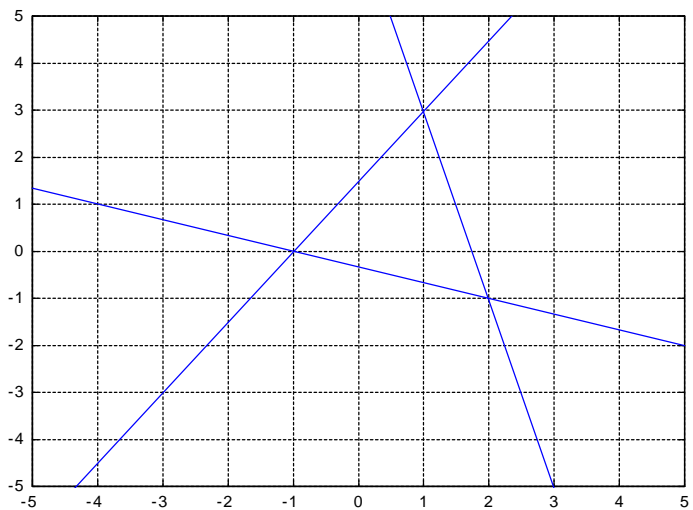


One solution:
 $x = 2$
 $y = -1$

Chapter 1, section 2, problem 1e program file Ch1s2pb01e.m

```
plotline(4,1,7)  
hold on  
plotline(3,-2,-3)  
plotline(1,3,-1)  
grid  
hold off
```

Result in Matlab



No solutions:
The three lines
do not intersect
at a common
point.